

12 • The Gas Laws

BOYLE'S LAW

Boyle's Law states that the volume of a gas varies inversely with its pressure if temperature is held constant. (If one goes up, the other goes down.) We use the formula:

$$P_1 \times V_1 = P_2 \times V_2$$

Solve the following problems (assuming constant temperature). Assume all number are 3 significant figures.

1. A sample of oxygen gas occupies a volume of 250 mL at 740 torr pressure. What volume will it occupy at 800 torr pressure?

~~250 mL~~

$$P_1 V_1 = P_2 V_2 \quad \frac{250 \cdot 740}{800} = V_2$$

$$\frac{250 \times 740}{800} = \frac{800 V_2}{800}$$

$$231 \text{ mL}$$

2. A sample of carbon dioxide occupies a volume of 3.50 Liters at 125 kPa pressure. What pressure would the gas exert if the volume was decreased to 2.00 liters?

$$\frac{3.5 \text{ L} \times 125 \text{ kPa}}{2.00} = 2.00 P_2$$

$$219 \text{ kPa}$$

3. A 2.00-Liter container of nitrogen had a pressure of 3.20 atm. What volume would be necessary to decrease the pressure to 1.00 atm?

$$\frac{2(3.20)}{1} = 1 \text{ atm } V_2$$

$$6.4 \text{ L}$$

4. Ammonia gas occupies a volume of 450 mL as a pressure of 720 mmHg. What volume will it occupy at standard pressure (760 mmHg)?

$$\frac{450 \times 720}{760} = 426 \text{ mL}$$

5. A 175 mL sample of neon had its pressure changed from 75.0 kPa to 150 kPa. What is its new volume?

$$\frac{175 \times 75}{150} = 87.5 \text{ mL}$$

6. A sample of hydrogen at 1.50 atm had its pressure decreased to 0.50 atm producing a new volume of 750 mL. What was the sample's original volume?

$$1.50 V_1 = \frac{0.50(750)}{1.50}$$

$$250 \text{ mL}$$

7. Chlorine gas occupies a volume of 1.20 liters at 720 torr pressure. What volume will it occupy at 1 atm pressure?

$$\frac{1.20 \times 720}{760} = \frac{720 V_2}{760} = 1.14 \text{ L}$$

8. Fluorine gas exerts a pressure of 900 torr. When the pressure is changed to 1.50 atm, its volume is 250 mL. What was the original volume?

$$V_1 \cdot 900 = \frac{1.5 \cdot 250}{900}$$

$$.42 \text{ atm}$$

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CHARLES'S LAW

Charles' Law states the volume of a gas varies directly with the Kelvin temperature, assuming the pressure is constant. We use the following formulas:

V = Liters T = Kelvin

$$\frac{V_1}{T_1} = \frac{V_2}{T_2} \quad \text{or} \quad [V_1 \times T_2 = V_2 \times T_1]$$

K = °C + 273

cross multiplication

always convert

Solve the following problems assuming a constant pressure. Assume all numbers are 3 significant figures.

1. A sample of nitrogen occupies a volume of 250 mL at 25 °C. What volume will it occupy at 95 °C?

$$\frac{.250L}{25+273K} = \frac{.250L}{298} = \frac{\quad}{368} \quad \boxed{.31L}$$

2. Oxygen gas is at a temperature of 40 °C when it occupies a volume of 2.30 Liters. To what temperature should it be raised to occupy a volume of 6.50 Liters?

$$6.5L / 313K = 2.3L / T_2 \quad \boxed{111K}$$

3. Hydrogen gas was cooled from 150 °C to 50 °C. Its new volume is 75.0 mL. What was its original volume?

$$V_1 / 423K = .075 / 323K \quad \boxed{.098L \text{ or } 98mL}$$

4. Chlorine gas occupies a volume of 25.0 mL at 300 K. What volume will it occupy at 600 K?

$$.025L / 300K = V_2 / 600K \quad \boxed{.05L \text{ or } 50mL}$$

5. A sample of neon gas at 50 °C and a volume of 2.50 Liters is cooled to 25 °C. What is the new volume?

$$2.5L / 323K = V_2 / 298K \quad \boxed{2.3L}$$

6. Fluorine gas at 300 K occupies a volume of 500 mL. To what temperature should it be lowered to bring the volume to 300 mL?

$$.5L / 300K = .3L / T_2 \quad \boxed{180K}$$

7. Helium occupies a volume of 3.80 Liters at -45 °C. What volume will it occupy at 45 °C?

$$3.8 / \cancel{278K} = V_2 / 318K \quad \boxed{5.3L}$$

228K

8. A sample of argon gas is cooled and its volume went from 380 mL to 250 mL. If its final temperature was -55 °C, what was its original temperature?

$$.38L / T_1 = .25 / 218K \quad \boxed{331K}$$

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THE IDEAL GAS LAW

$C^{\circ} + 273 = K$

$$\frac{g}{V} = D = \frac{PM}{RT}$$

PV = nRT where

P = pressure in atmosphere
 V = volume in liters
 n = number of moles of gas
 R = Universal Gas Constant = 0.0821 L·atm/mol·K
 T = Kelvin temperature

760 torr = 1
 760 mmHg = 1
 101.3 kpa = 1 atm

- How many moles of oxygen will occupy a volume of 2.50 liters at 1.20 atm and 25 °C?
 $n = .12 \text{ moles } O_2$
 $V = 2.5$
 $P = 1.20 \text{ atm}$
 $T = 298 \text{ K}$
 $2.5(1.2) = n(0.0821)(298)$
 $n = \frac{2.5(1.2)}{(0.0821)(298)}$
- What volume will 2.00 moles of nitrogen occupy at 720. torr and 20.°C?
 $V = 51 \text{ L}$
 $n = 2$
 $P = 720 \text{ torr} / 760 = .947$
 $T = 20 + 273 = 293 \text{ K}$
 $.947(V) = \frac{2(.0821)(293)}{.947}$
- What pressure will be exerted by 25.0 g of CO₂ at temperature of 25 °C and a volume of 500. mL?
 $P = 2.8 \text{ atm}$
 $25 + 273 = 298$
 $\frac{25 \text{ g}}{500 \text{ L}} = \frac{P(44)}{(.0821)(298)}$ — 44g/mol (Periodic Table) $\frac{1223.29}{44}$
- At what temperature will 5.00 g of CH₄ exert a pressure of 900. torr at a volume of 750. mL?
 157 K
 $900/760 = 1.18$
 5.00 g
 $760(1.18) = \frac{.07(0.0821)T}{157}$
 157 K
- What is the density of NH₃ at 800. torr and 25 °C?
 $800/760 = 1.1$
 $\frac{17(1.1)}{(.0821)(298)} = .76 \text{ g/L}$
- If the density of a gas is 1.2 g/L at 745 torr and 20.°C, what is its molar mass?
 29.5 g/mol
 $P = 745/760 = .98$
 $1.2 = \frac{.98M}{(.0821)(293)}$
 $(1.2 \times .0821 \times 293) = 29.5 \text{ g/mol}$
- How many moles of nitrogen gas will occupy a volume of 347 mL at 6680 torr and 27 °C?
 $n = .12 \text{ moles } N_2$
 $V = .347 \text{ L}$
 $P = 6680/760 = 8.79$
 $T = 27 + 273 = 300 \text{ K}$
 $8.79(.347) = n(0.0821)(300)$
 $n = \frac{8.79(.347)}{(.0821)(300)}$
- What volume will 454 grams (1 lb) of hydrogen occupy at 1.05 atm and 25 °C?
 $5,289 \text{ L}$
 $25 + 273 = 298 \text{ K}$
 $\frac{454}{V} = \frac{1.05(2)}{(.0821)(298)}$ — 2 - H₂ - P.T. $\frac{454 \text{ g}}{(.0821)} = V$
- Find the number of grams of CO₂ that exert a pressure of 785 torr at a volume of 32.5 L and a temperature of 32 °C.
 59 g
 $785/760 = 1.03 \text{ atm}$
 $32^{\circ}C + 273 = 305 \text{ K}$
 $\frac{g}{32.5 \text{ L}} = \frac{1.03 \text{ atm} (44 \text{ g/mol } CO_2)}{(.0821)(305 \text{ K})} \cdot 32.5 \text{ L}$
- An elemental gas has a mass of 10.3 g. If the volume is 58.4 L and the pressure is 758 torr at a temperature of 2.5 °C, what is the gas?
 $4.35 \text{ g} \rightarrow \text{P.T.} \rightarrow \text{HELIUM}$

758/760 $\frac{10.3 \text{ g}}{58.4 \text{ L}} = \frac{.997(M)}{(.0821)(293.5 \text{ K})}$
 $2.5 + 273$
 $.18(.0821)(293.5 \text{ K}) = \frac{.997(M)}{.997}$
 997